

Geocentric to Geodetic Transformation (Vincenty 1980)

$$b = a(1 - f) \quad (1)$$

$$P^2 = X^2 + Y^2, \quad r^2 = P^2 + Z^2 \quad (2) \text{ \& } (3)$$

$$h' = r - a + \frac{(a - b)Z^2}{r^2} \quad (4)$$

$$a' = a + h', \quad b' = b + h' \quad (5) \text{ \& } (6)$$

$$\tan \phi' = \left(\frac{a'}{b'} \right)^2 \left(\frac{Z}{P} \right) \left[1 + \frac{1}{4} \frac{e^4 h' a (Z^2 - P^2)}{a'^4} \right] \quad (7)$$

$$\cos^2 \phi' = \frac{1}{1 + \tan^2 \phi'}, \quad \sin \phi' = \cos \phi' \tan \phi' \quad (8) \text{ \& } (9)$$

$$T = \frac{(P - h' \cos \phi')^2}{a^2}, \quad U = \frac{(Z - h' \sin \phi')^2}{b^2} \quad (10) \text{ \& } (11)$$

$$h = h' + \frac{1}{2} \left[\frac{T + U - 1}{\frac{T}{a} + \frac{U}{b}} \right] \quad (12)$$

$$\phi = \tan^{-1} \left[\left(\frac{a}{b} \right)^2 \frac{(Z - e^2 h \sin \phi')}{P} \right] \quad (13)$$

$$\lambda = \tan^{-1} \left(\frac{Y}{X} \right) \quad (14)$$

Another method would be to iterate for an "exact" solution as described by Leick (1990) using equations 6.31 to 6.36.